

Production of black holes and string balls in a two-dimensional split-fermion model

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ABSTRACT: We present cross-sections for the black hole and string ball production in proton-proton collisions in a TeV-scale gravity model with split fermions in two dimensions. The cross-section for black hole and string ball production in the split-fermion model is smaller than in the non-split-fermion model. The drop of the cross-section for the string ball production can be one to two orders of magnitude with the increase of the width of the brane from $L = 0$ to 15 TeV^{-1} . The cross-section for string ball production in two-dimensional split fermion model reduces more in comparison to black holes. Black holes are quite hard to be observed at the LHC. In fact, taking into account the current experimental limits on the fundamental Planck scale, black holes cannot be produced at the LHC. Cross-section for string ball production depends significantly on string coupling constant, making it very model dependent. We investigate the range of values of string coupling constant from 0.02 to 0.4. There has been no evidence for production of string balls at $\sqrt{s} = 8 \text{ TeV}$. A two-dimensional split fermion model with a extremely thick brane can account for the absence of signature of string balls for a world with the value of fundamental Planck scale even as low as 1 TeV.

KEYWORDS: black holes, string balls, split fermions, extra dimensions, quantum gravity

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1 Introduction

Models of large or warped [1–5] extra dimensions allow the fundamental scale of gravity to be as low as the electroweak scale, providing us with a low-scale gravity model. With a black hole solution finally discovered in Randall-Sundrum model [6–8], warped extra dimensions can have validation as well. One of the predictions of low-scale gravity models is the possibility of black hole production in particle collisions with energies above the gravity scale, such as in proton-proton collisions at the Large Hadron Collider (LHC) for TeV-scale gravity.

Low-scale quantum gravity models have some unacceptable predictions, such as fast proton decay, large $n\bar{n}$ oscillations, large mixing between leptons, etc. A solution to some of the unacceptable predictions of low-scale quantum gravity models is the split-fermion model [9, 10]. In this model, the Standard Model particles are confined to a “thick” brane extending in the higher dimensional bulk space. In the simplest case, this thickness is one-dimensional, and quarks and leptons live on different slices of this thick brane. The split-fermion model also has some other advantages. The model allows a geometric interpretation of the observed fermion masses. Namely, the effective four-dimensional Yukawa couplings can be viewed as overlaps of the wave functions between two different chiral fermions and is lower as their relative distance in the split-fermion dimension increases. In a one split-fermion dimension model, it is not possible to obtain sufficient CP violation in accordance with the experimental data. Considering two split-fermion dimensions, i.e., a six-dimensional Standard Model [11], one can find an example where all the quark masses and the mixing angles, as well as the required strength of CP violation in quark sector are reproduced. In order to make serious predictions, one needs to work within the context of realistic phenomenologically valid models. We consider that, a two-dimensional split fermion model is such a model for a TeV-scale quantum gravity.

The analysis of black hole production in colliders range from using a simple πr_g^2 form for the cross-section, where r_g is the gravitational radius of the black hole formed in the parton scattering process [12–14], to calculations based on classical general relativity using the trapped-surface approach [15–17]. The effects of finite particle size [18, 19], angular momentum [20–24], and electric charge [25, 26] on the cross-section are sometimes included in limited form.

If the black hole is formed with mass not too close to the Planck scale, it is anticipated to decay by emitting Hawking radiation [27]. If the black hole is produced at the LHC, it would decay to final states with a relatively high multiplicity. The theory of black hole evaporation is based on a semiclassical description involving quantum fields on classical space-time backgrounds. Although in the classical general relativity theory black holes can only absorb and not emit particles, in the semiclassical description black holes create and emit particles as if they were hot bodies. The radiation from the black hole is thermal, meaning information would be permanently lost inside the event horizon, and there would be no S -matrix to take an initial pure state to a final pure state, violating unitarity in quantum mechanics [28]. Although it has been suggested that some new dynamics provided by quantum gravity at short distances would resolve this issue at the final stage of the black hole evaporation, it is widely accepted [29, 30] now that most of the information comes out with the bulk of the radiation to give an S -matrix, allowing the number of possible microstates of the black hole to be proportional to the exponential of its entropy. If so, the black hole could make a transition to a highly-excited string state as it evaporates.

This string theory motivated scenario provides a convincing picture of the evolution of a black hole at the last stages of its evaporation. As the black hole shrinks, it eventually reaches the “correspondence point” $M_{min} \sim M_s/g_s^2$, (where M_s is the string scale related to the fundamental Planck mass and g_s is the dimensionless string coupling constant), and makes a transition to a configuration dominated by a highly-excited long string called a string ball [31–33]. String balls evaporate thermally at the Hagedorn temperature and give rise to high-multiplicity events containing hard primary photons and charged leptons, which have negligible standard-model background [34]. The result is that, the evaporating black hole leaves no stable remnant.

If the Planck scale is a few TeV, the mass of the black hole has to be close to the maximum LHC energy for it to be described by general relativity. Because of the steeply falling parton distribution functions with increasing mass, this leads to a black hole production cross-section that is significantly reduced at the LHC. However, because of the correspondence between black holes and string balls, black hole production is dual to the production of a highly-excited long string state. Thus, if the string scale and the Planck scale are a few TeV in large extra dimensions, we might expect TeV-scale string physics at the LHC. String balls would be expected to be produced at the LHC much more than black holes [35–38].

Black holes and string balls have been searched for in proton-proton collisions at the LHC. ATLAS collaboration has performed a search for an excess of events with multiple high transverse momentum objects including charged leptons and jets, using 20.3 fb⁻¹ of proton-proton collision data recorded by the ATLAS detector at the Large Hadron Collider in 2012 at a centre-of-mass energy of $\sqrt{s} = 8$ TeV [39]. No excess of events beyond Standard

Model expectations have been observed (also see [40, 41]). The CMS collaboration [42, 43] has published using up to 4.7 fb^{-1} of 7 TeV data. In addition, CMS has published a result using 3.7 fb^{-1} of 8 TeV collision data [44]. In all cases, agreement with the expected Standard Model backgrounds were obtained. The CMS experiment has excluded up to a black hole mass of 3.5-4.5 TeV in a variety of theoretical models.

In this paper, we present cross-sections for the black hole and string ball production for proton-proton collisions in a TeV-scale gravity model with split fermions in two dimensions. We compare the cross-section for black hole and string ball production in particle collisions in the non-split-fermion model to a two-dimensional split-fermion model. We illustrate that the split-fermion model affects the string ball cross section more than the black hole cross-section. Given the lack of signature of black holes or string balls for the centre-of-mass energy $\sqrt{s} = 8 \text{ TeV}$ at the LHC, limits on the value of the fundamental Planck scale can be imposed. These limits depend on the width of split fermion dimension and the value of the string coupling constant. We investigate the range of values of string coupling constant from 0.02 to 0.4. Furthermore, no evidence for production of string balls at $\sqrt{s} = 8 \text{ TeV}$ suggests that if our world has extra dimensions with the fundamental scale of multidimensional gravity being between one to two TeV units then, it should be something like a two-dimensional split fermion model with a “thick” brane.

This paper is organized as follows: In Sec. 2 we define the model we are considering, and in Sec. 3 we present our numerical results, and their discussion. We have largely used the BlackMax Monte Carlo event generator [45, 46] for our computations. We present some of the details for running of the BlackMax code in Appendix.

2 Black holes and string balls

2.1 Two-dimensional split-fermion model

In this paper, we consider both black hole and string ball production cross-sections in a split-fermion model with two split-fermion dimensions. Two split-fermion dimensions helps solve some of the unacceptable predictions of the low-scale quantum gravity models, as well as providing us with an example where all the quark masses, the mixing angles, and the required strength of CP violation in quark sector can be reproduced [11].

In the simplest split-fermion model [47], only one split-fermion dimension is considered, which gives the five-dimensional Standard Model with the fermions being localized in the extra dimensional brane, while gauge bosons and Higgs fields can propagate in the extra dimension. If one assumes that fermions have a Gaussian distribution in the fifth dimension, and one universal Yukawa coupling to the bulk Higgs field, one can find a unique configuration of the Standard Model fermions positions which can explain the Yukawa mass hierarchies by displacing the left-handed and right-handed components of the Standard Model fermions without imposing new symmetries [47]. This configuration fits all quark and lepton masses, and mixing angles of the four-dimensional Standard Model. However, if one considers only one split-fermion dimension then, it is not possible to obtain sufficient CP violation in accordance with the experimental data while having one universal coupling to

the bulk Higgs field. Considering two split-fermion dimensions, i.e., a six-dimensional Standard Model [11], one can find an example where all the quark masses and the mixing angles, as well as the required strength of CP violation in quark sector are reproduced, even though this may not be a unique configuration. Note that, it is also possible to produce the required CP violation in the five-dimensional Standard Model (one-dimensional split-fermion model) by having different Yukawa couplings for up-type and down-type quarks [48].

We assume that Standard Model fermions have different positions in the extra two split-fermion dimensions, and common Gaussian profiles about these positions. Thus, in the two-dimensional split-fermion model

$$\Psi(\vec{x}) = \sqrt{\frac{2}{\pi}} \mu \exp[-\mu^2(x_5^2 + x_6^2)] \psi(x_0, x_1, x_2, x_3), \quad (2.1)$$

where, x_5 and x_6 are the split-fermion dimensions, and ψ is a canonically normalized massless left-handed four-dimensional fermion wave function. For simplicity, we consider the same Gaussian width $\sqrt{2}/\mu$ for both split-fermion dimensions x_5 and x_6 . The location of the fermion wave functions are taken from Ref. [11] and shown in Table 1.

Quark type	$(u, d)_L$	$(c, s)_L$	$(t, b)_L$
Position (μ^{-1})	(5.941,0)	(-4.008,0)	(0,0)
Quark type	u_R	c_R	t_R
Position (μ^{-1})	(-8.347,0)	(1.815,0)	(-0.941,0)
Quark type	d_R	s_R	b_R
Position (μ^{-1})	(-8.421,0)	(2.219,2.332)	(-1.253,2.767)

Table 1. Location of left-handed and right-handed quarks inside the thick brane in units of μ^{-1} in a model with two split-fermion dimension[11].

Next, we discuss the constraints on the parameter space of our model. The width μ^{-1} of the wave functions should be smaller than the brane thickness L but, larger than the scale of the ultraviolet cutoff $1/M_*$:

$$L^{-1} < \mu < M_*. \quad (2.2)$$

A second condition is to have the four-dimensional Yukawa top coupling λ_t perturbative at M_* :

$$\frac{M_*}{L^{-1}} < 2\pi \left(\frac{4\pi}{\lambda_t} \right)^2 \approx \frac{992.2}{\lambda_t^2}. \quad (2.3)$$

For the field theory description to be valid through the wall $\mu^2 L < M_*$. Combined with Eq. (2.3) this gives

$$L_f < \frac{\mu}{L^{-1}} < \frac{31.5}{\lambda_t}. \quad (2.4)$$

Here, we consider $\lambda_t < 1$ or close to 1. The left hand side of the condition (2.4) restricts all the fermions to be accommodated inside the brane of width L , where $L_f = 14.362$ is the total distance between the position of d_R and $(u, d)_L$.

In Ref. [47], another condition is mentioned, i.e., $R^{-1} \sim L^{-1} > 100$ TeV. However, this constraint comes from the flavour changing neutral currents mediated by Kaluza-Klein gauge bosons in a compactified five-dimensional Standard Model, where the fifth dimension x_5 has been compactified on the orbifold S^1/Z_2 , a circle of radius R with the identification $x_5 \rightarrow -x_5$. This condition disfavors the scenario of TeV-strings [49] and will not be followed in this paper.

2.2 String balls versus black holes

In order to be able to neglect the quantum gravity effects which strongly modify the classical general relativistic black hole solutions, one must consider black holes of large number of states. We will assume the commonly used condition that, the entropy of the black hole must be greater than 25, or its mass $m > 5M_D$ [50]. We consider the mass $M_{\min}^c = 5M_D$, to be the minimum classical mass of the black hole, i.e., the minimum mass at which the classical general relativistic description is still valid. In this case, the window for the production of classical black hole is small.

If one wishes to consider the LHC results on the minimum limits on the Planck scale to date [51], high mass black holes ($m > 5M_D$) cannot be produced in three and four extra dimensions for $\sqrt{s} = (8-14)$ TeV. This is because the black hole cross-section drops with increasing black hole mass, due to the steeply falling parton density distributions in the protons with increasing parton centre-of-mass energy. The experimental limits on the fundamental Planck scale in [51] are set using only the direct graviton emission searches from the LHC experiments. However, for large number of extra dimensions the limits are still not so stringent. Other direct limits come from non-observation of black hole events come from the simplest models (e.g. no split-splitting of fermions), which we believe cannot be taken at face value (in order to make reliable predictions one has to work with phenomenologically valid models without fast proton decay, large neutron-antineutron mixing, large mixing between leptons etc). Therefore, every number in the Table 1 in [51] has to be taken in the proper context. We do not consider these limits in our paper. In the case that, the fundamental Planck scale is greater than the current experimental limits, one has to apply a proper vertical cut in our figures at the corresponding value of M_D .

The string entropy in any number of dimensions is proportional to the mass of string

$$S \sim \frac{m}{M_s}, \quad (2.5)$$

where M_s is the string scale related to the fundamental Planck scale M_D . For example, if we consider a model with n large extra dimensions ($n \leq 6$) and q small dimensions ($q = 6 - n$) compactified on a q -torus of radius equal to the string length $l_s \sim 1/M_s$ then,

$$M_s = \frac{g_s^{2/(n+2)}}{(2\pi)^{(n-6)/(n+2)}} M_D, \quad (2.6)$$

where g_s is the dimensionless string coupling constant in weakly-coupled string theory [35]. For the string theory to be perturbative, g_s must be less than unity. An example of a

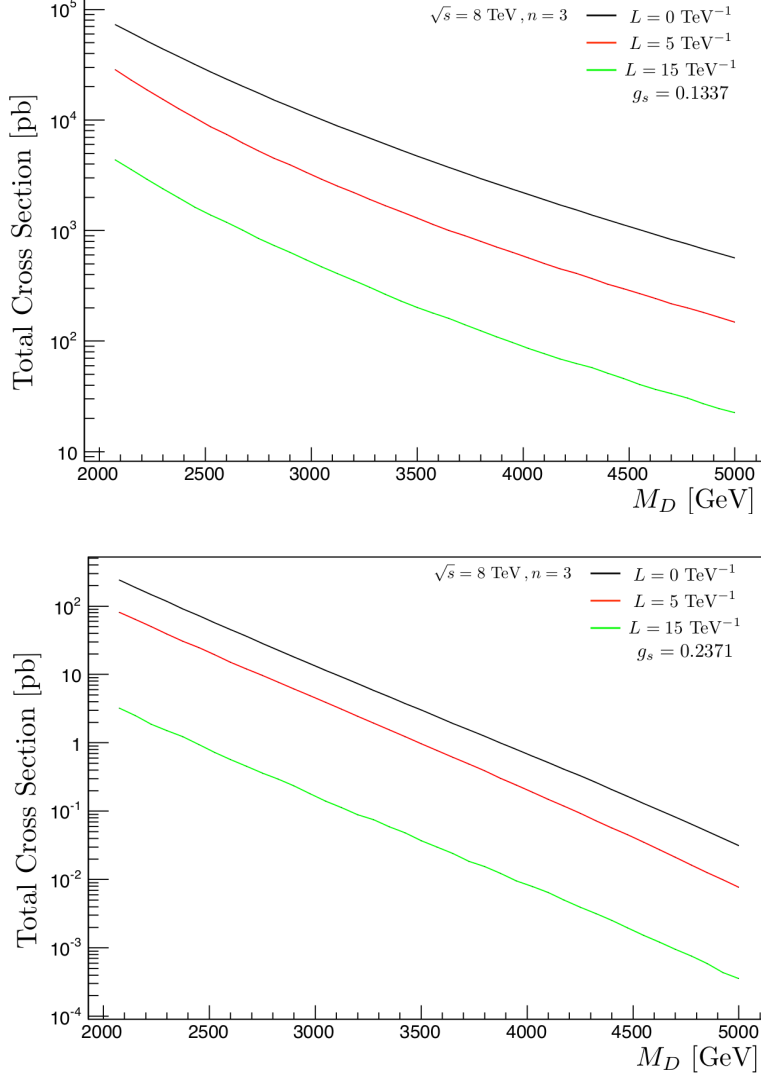


Figure 1. The first plot shows total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 3$ and $L=0, 5, 15$ TeV $^{-1}$ and string coupling constant $g_s = 0.1337$. The second plot shows total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 3$ and $L=0, 5, 15$ TeV $^{-1}$ and string coupling constant $g_s = 0.2371$.

typical value of g_s in theories with large extra dimensions with values of g_s between 0.02 and 0.2 have been discussed in [52]. There are other results [13, 14] which, they take into account string coupling constant g_s to be close to one. Relation (2.6) is model dependent, with respect to the specific compactification schemes and the string theory model under consideration. For example, one can find a different relation between M_s and M_D [36]. Therefore, we write the relation (2.6) in the following form:

$$M_s = \gamma g_s^{2/(n+2)} M_D, \quad (2.7)$$

where, the exact numerical coefficient γ is model dependent.

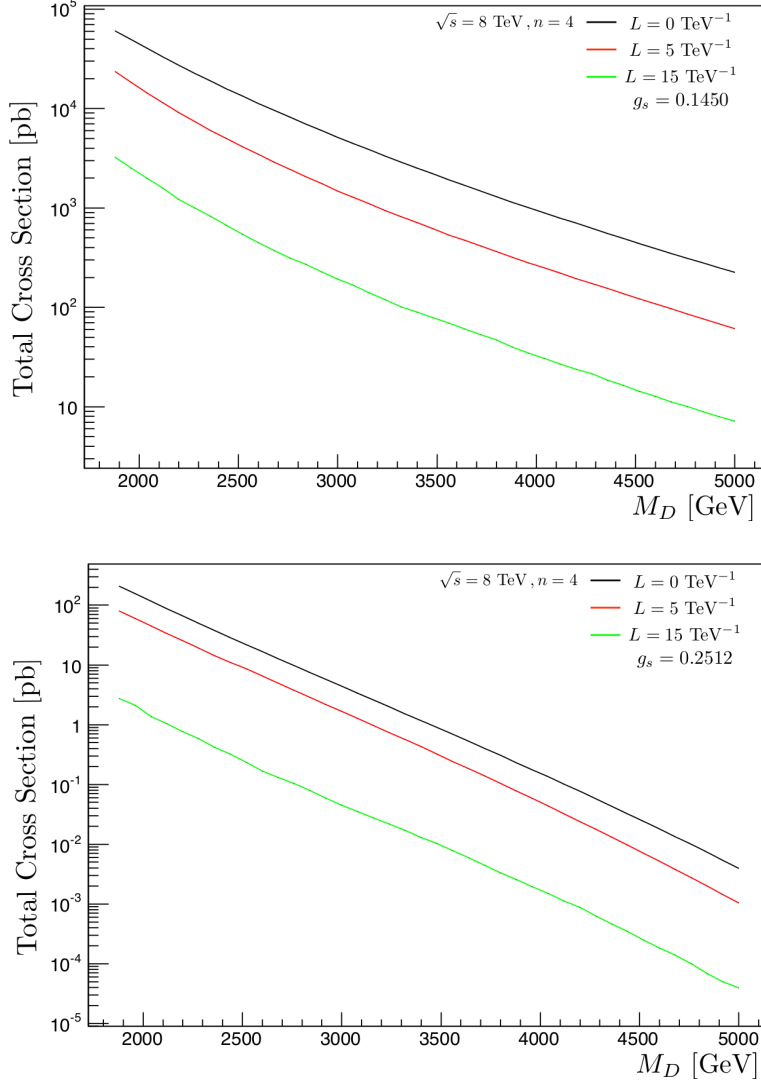


Figure 2. The first plot shows total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 4$ and $L=0, 5, 15$ TeV $^{-1}$ and string coupling constant $g_s = 0.1450$. The second plot shows total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 4$ and $L=0, 5, 15$ TeV $^{-1}$ and string coupling constant $g_s = 0.2512$.

We assume that, in a quantum theory of gravity there will be a space of states $H(E, J)$ which describes the possible quantum states of the gravitational field which have energy E and angular momentum J . Assume that, there is a region in the space of states $H(E, J)$, which contains the quantum states which correspond to the black hole $H_{\text{BH}}(E, J)$, and a region $H_s(E, J)$ which, contains the corresponding excited states of the strings, and that the logarithm of the number of states in the string region is proportional to the relevant entropy. Further, we assume that, the rates for transitions between the states in the black hole and the string regions are on the order of the rates for transitions between states within the regions, and that all of these rates are on the order of $1/E$. Given this, one may expect that the relative entropy of states in the two regions gives the relative probabilities that

the system will be found in each region, independently of the initial conditions.

Suppose that, a black hole of mass m is formed in the collider with $M_D < M_{\min}^c < m$. Also consider that, the black hole is in empty space and evaporating according to the Hawking radiation process. As the energy decreases we consider the probability for the black hole state to make a transition to one of the massive string states. There exists a critical value of the mass where the entropies are equal, above this value the entropy of the black hole is greater than the entropy of the string ball, and the black hole state is the favourable state, below this value of mass the string state is the favourable state. Thus, it is entropically favourable for the black hole to make a transition to one of the massive modes of the string at the correspondence point, where the entropies are equal,

$$m \sim \frac{M_s}{g_s^2}. \quad (2.8)$$

We call this minimum mass (M_s/g_s^2) the stringy minimum mass of the black hole M_{\min}^s . The black hole leaves no remnant, i.e., the black hole can evaporate completely, avoiding the singularity that is inevitable in the semiclassical picture [31].

Going back to our first assumption that, in a quantum theory of gravity there will be a space of states $H(E, J)$ which describes the possible quantum states of the gravitational field, we can view black holes and string balls as describing different forms of the same gravitational object at different energies. Thus, we expect that for centre-of-mass energies less than M_{\min}^s string balls to be produced at the LHC, rather than black holes. Namely, the correspondence between the black hole and string ball also suggests that, string balls production is dual to the black hole production, and the production cross-section for string balls will match the black hole cross-section at the correspondence point [14]. In this paper, we equate the stringy minimum mass of black hole M_{\min}^s to the classical minimum mass of black hole M_{\min}^c . One may still hope to copiously produce black holes lighter than $m > 5M_D$, and that, the quantum corrections will not be disastrous. For this reason, in one of our figures we consider the cross-section for string ball and black hole production in the case that $M_{\min}^c = M_{\min}^s = 3M_D$.

The cross-section and event characteristics for black holes and string balls in higher dimensional models with no split-fermions have already been considered [38]. In [38], M_{\min}^c is taken to be $5M_D$ which is supported by their thermodynamic and Compton wavelength argument. The cross-section for the production of black holes and their angular momentum distribution in a one dimensional split-fermion model have been studied [53]. It was shown that, for a given value of the Planck scale, the total production cross-section is reduced as compared to the model with non-split-fermions. Here, we have considered string balls and black holes into a two-dimensional split-fermion model for the first time. To calculate the cross-section of the black hole or string ball production we use the equation (21) of [53] which is implemented in BlackMax code.

3 Numerical results

The production of black holes and string balls in particle collisions depend on the following parameters:

1. The parameters of the higher-dimensional space: number of extra dimensions n and the D -dimensional fundamental Planck scale M_D . We use the PDG definition of the Planck scale [54].
2. The parameters of the split-fermion model: the number of split-fermion dimensions, (we consider a two-dimensional split-fermion model), the width of the fermion wave functions, the width of the split-fermion brane L , and the location of the fermions in the split-fermion brane taken from Table 1.
3. The parameters of the particle collisions: the type and centre-of-mass energy of the colliding partons. We consider proton-proton collisions at the LHC energies of 8 TeV, and 14 TeV. This allows us to compare our results with the current and the future run of the LHC. We use the CTEQ6.1M parton distribution functions [55].
4. The mass, momentum, and angular momentum loss factors in the inelastic collision before the formation of the black hole.
5. The string ball parameters: the string scale M_s , the string coupling constant g_s , and the minimum mass of the string ball M_{ms} , which we take to be $3M_s$.

Typically, the scales of the problem have the following hierarchy

$$M_s < M_{ms} < M_D < \frac{M_s}{g_s^2}. \quad (3.1)$$

Other parameters of the simulation are the minimum classical mass of the black hole M_{min}^c and the stringy minimum mass of black hole M_{min}^s . It is natural to equate the stringy minimum mass of black hole M_{min}^s to the classical minimum mass of black hole M_{min}^c . In other words,

$$M_{min}^s \sim \frac{M_s}{g_s^2} = M_{min}^c = 5M_D. \quad (3.2)$$

By this condition and Eq. (2.7), the string scale M_s and the string coupling constant g_s are fixed, if we know γ .

In what follows we investigate the dependence of the cross-section production of string balls and black holes on the above parameters.

We will not be able to cover all the range of parameter space, rather we try to simply illustrate and discuss the sensitivity of the production cross-section on some of the parameters. We have used the BlackMax code for our numerical computation, for details see Appendix A.

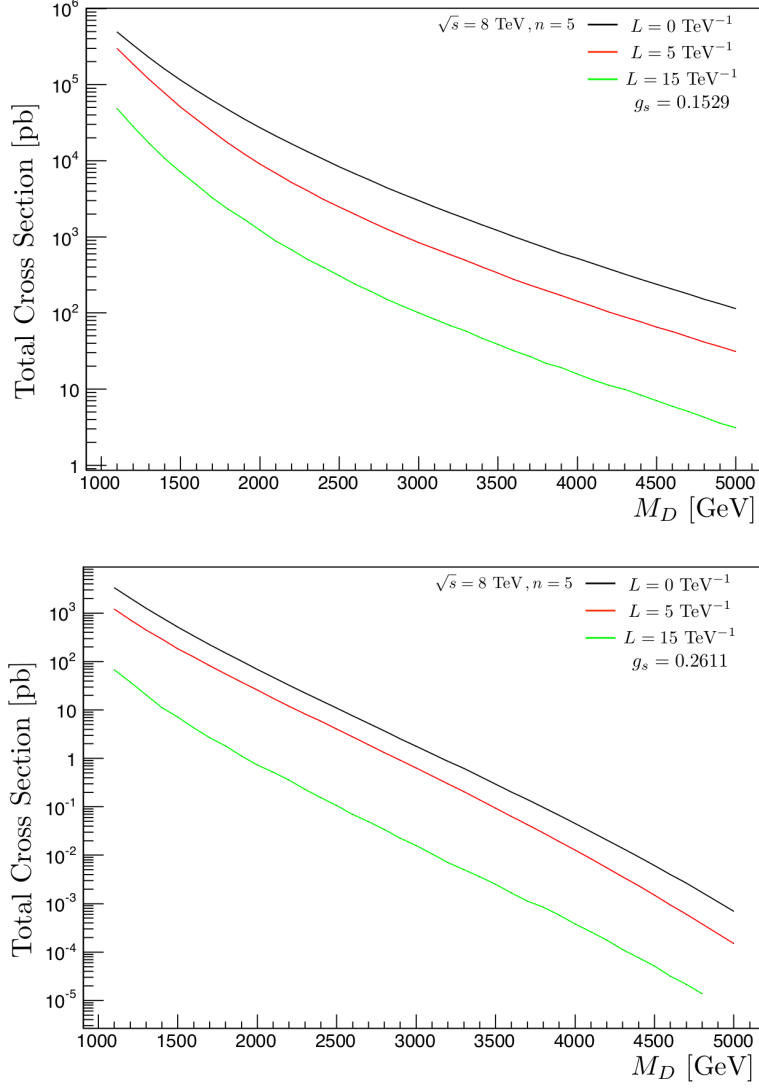


Figure 3. The first plot shows total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 5$ and $L=0, 5, 15$ TeV $^{-1}$ and string coupling constant $g_s = 0.1529$. The second plot shows total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 5$ and $L=0, 5, 15$ TeV $^{-1}$ and string coupling constant $g_s = 0.2611$.

3.1 Discussion

We have considered the cross-section for black hole and string ball production in proton-proton collisions in a two-dimensional split-fermion TeV-scale gravity model.

The cross-section of string ball and black hole production decrease as M_D increases. In all the following figures, we do not consider values of M_D , where the cross-section drops below about 10^{-5} pb. At the integrated luminosity of 20.3 fb^{-1} , for the run of the LHC at $\sqrt{s} = 8$ TeV [39], this cross-section corresponds to no events. In the figures 1–8, we consider centre-of-mass energy $\sqrt{s} = 8$ TeV. The figures 1–7 illustrate the dependence of the cross-section for string ball production versus M_D to many different parameters of the

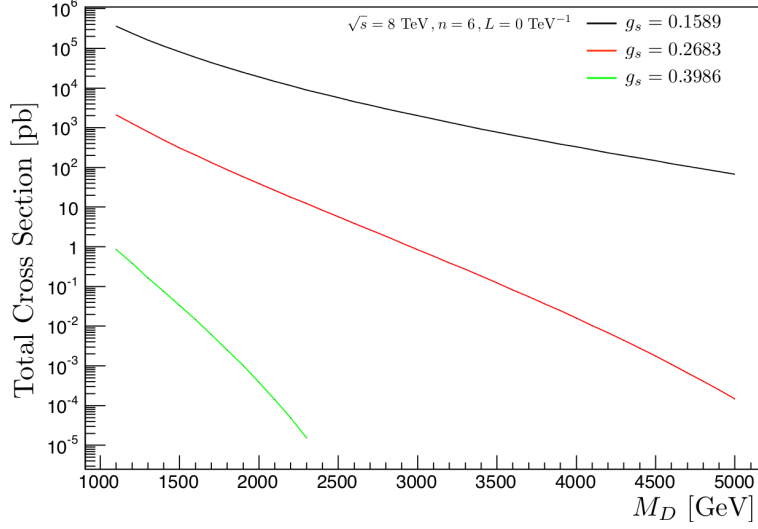


Figure 4. Total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 6$ and $L=0$ TeV^{-1} and different values of string coupling constant (g_s).

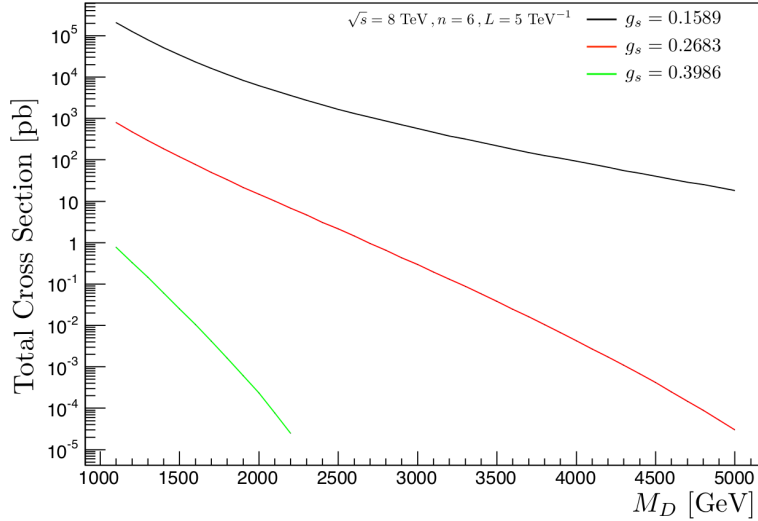


Figure 5. Total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 6$ and $L=5$ TeV^{-1} and different values of string coupling constant (g_s).

theory and especially to the string coupling constant (g_s). In the figures 1–3, we can see the cross-section of string ball production for different number of extra dimensions and different values of L . In these figures, we take into account two different values of g_s , the first one is calculated for parameter $\gamma = 0.2$, and the second one is calculated for $\gamma = 0.5$. The cross-section of string ball production significantly depends on value of g_s , therefore, is model dependent drastically. One of the goals of this paper is to investigate the relation between the cross-section and g_s . In particular, the range of values of the string coupling constant considered in [35] ($0.02 < g_s < 0.2$) is investigated. We can see from the graphs that, the cross-section of string ball production for the range of values of the string coupling

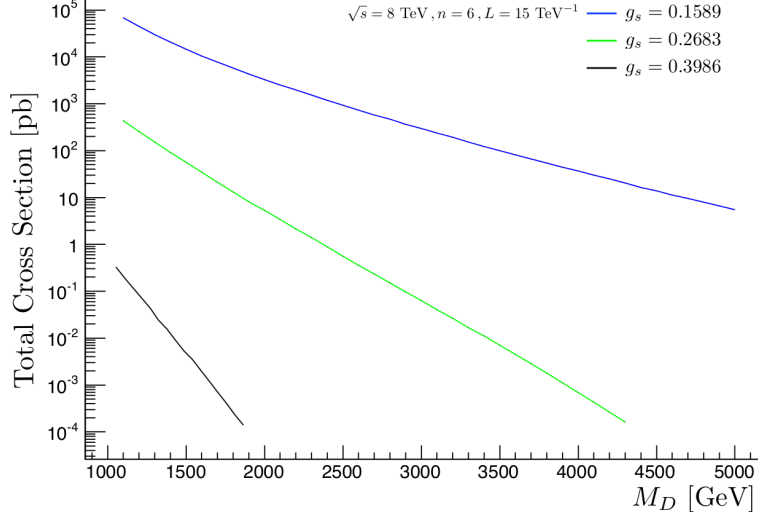


Figure 6. Total cross-section of string ball production for $\sqrt{s} = 8$ TeV, $n = 6$ and $L = 15$ TeV^{-1} and different values of string coupling constant (g_s).

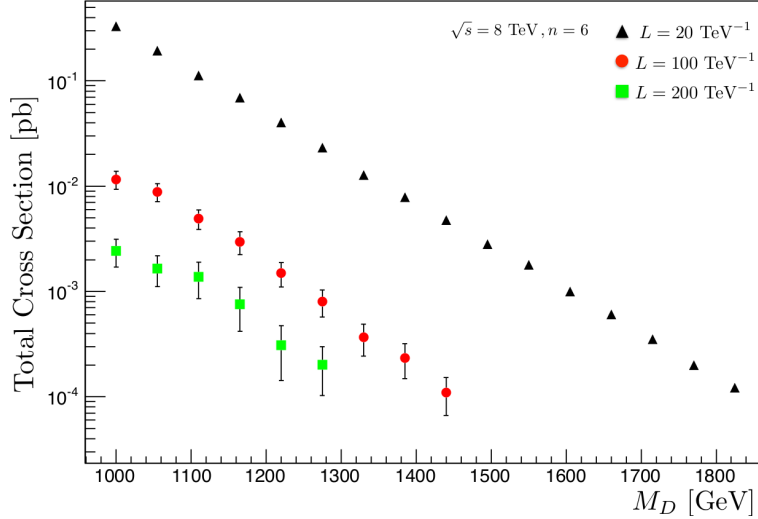


Figure 7. Total cross-section of string ball production for $n=6$, $\sqrt{s} = 8$ TeV, and for different values of L .

constant of $0.02 < g_s < 0.2$ is really high, even in the case that the centre-of-mass energy is only 8 TeV. By taking into account that we have no signature of string balls in the last run of the LHC [39], we conclude that g_s cannot be in that range if we want to have a theory of quantum gravity with low fundamental Planck scale. In the figures 4–6, the values of string coupling constant that we take into account are the following: $g_s = 0.1589$, $g_s = 0.2683$, and $g_s = 0.3986$. The first two values are calculated for parameter $\gamma = 0.2$ and $\gamma = 0.5$, respectively. For the last value of g_s , we let the value of γ to vary with the number of the extra dimensions according to the equation (2.6). The value of the width of the brane is constant for each figure and it is equal to $L = 0, 5, 15$ TeV^{-1} , respectively. These three

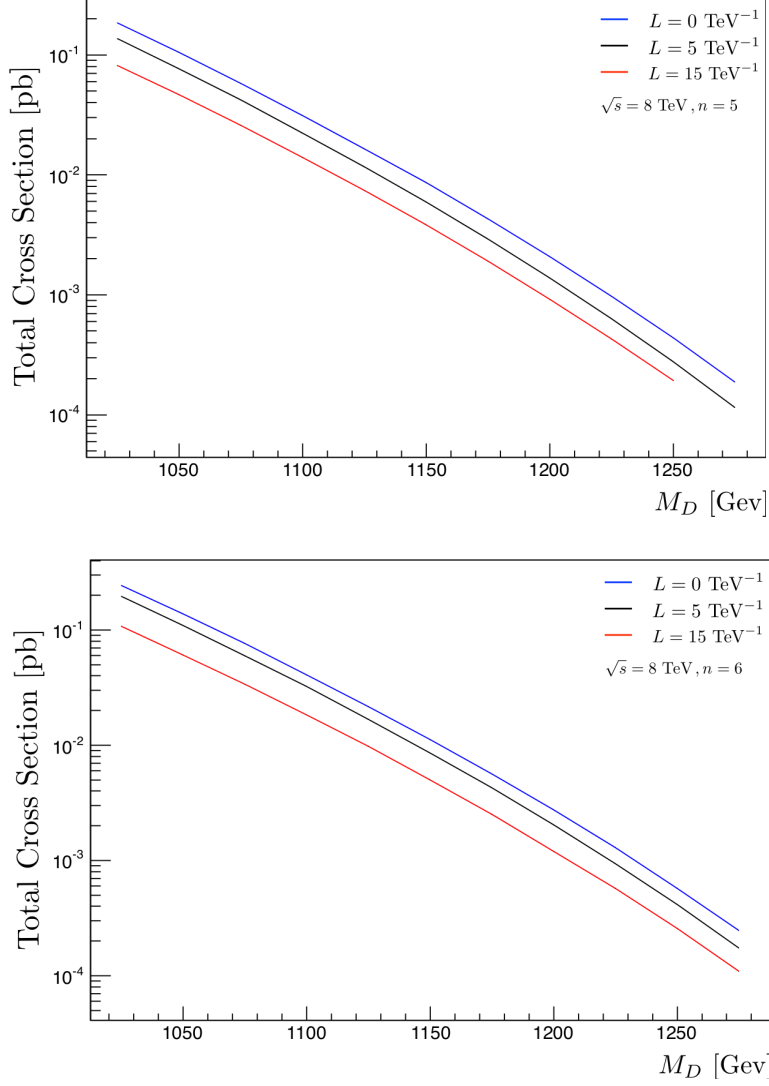


Figure 8. The first plot shows total cross-section of black hole production for $\sqrt{s} = 8$ TeV, $n = 5$ and $L=0, 5, 15$ TeV^{-1} . The second plot shows total cross-section of black hole production for $\sqrt{s} = 8$ TeV, $n = 6$ and $L=0, 5, 15$ TeV^{-1} .

figures are for the same number of extra dimensions ($n = 6$) and centre-of-mass energy (8 TeV).

Moreover, from figures 1–7, we see that the cross-section drops as the width of split fermion dimension L increases from $L = 0$ for non-split fermion model to $L = 15$ TeV^{-1} for a “thick” two-dimensional split fermion model. In the figure 7, we illustrate the cross section of the string ball production for extremely thick split fermion brane.

The last set of plots for the 8 TeV has to do with the cross-section of black hole production. In figure 8, we have considered the cross-section of the black hole production in $n = 5$ and $n = 6$ extra dimensions at centre-of-mass energy 8 TeV. Furthermore, we vary the number of the extra dimensions and the width of the split fermion brane L . Taking into

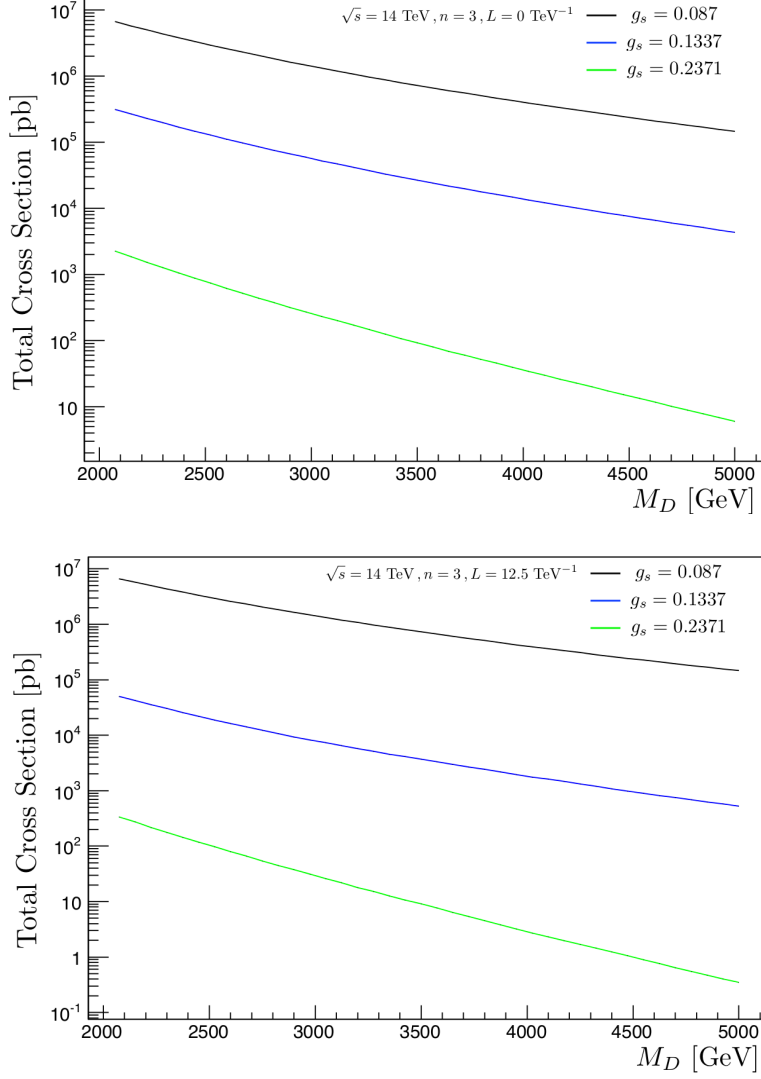


Figure 9. The first plot shows the total cross-section of string ball production for $\sqrt{s} = 14$ TeV, $n = 3$ and $L=0$ TeV^{-1} and different values of string coupling constant (g_s). The second plot shows the total cross-section of string ball production for $\sqrt{s} = 14$ TeV, $n = 3$ and $L=12.5$ TeV^{-1} and different values of string coupling constant (g_s).

account the current experimental limits on M_D for different number of dimensions, and the fact that the mass of the black hole has to be close to the maximum LHC energy for it to be described by general relativity ($m \geq 5M_D$), a black hole production cross-section is significantly reduced at the LHC.

In the figures 9–14, we consider centre-of-mass energy to be 14 TeV. The figures 9–11 illustrate more the dependence of the string ball cross-section in the split-fermion model and in the non-split-fermion model ($L = 0$) to the value of the string coupling constant g_s . From the figure 9, we can see that as the value of g_s increases the cross-section of string ball production drops faster as L increases. The figures 10 and 11 illustrate the dependence of the cross-section of the string ball production in various numbers of extra dimensions and L

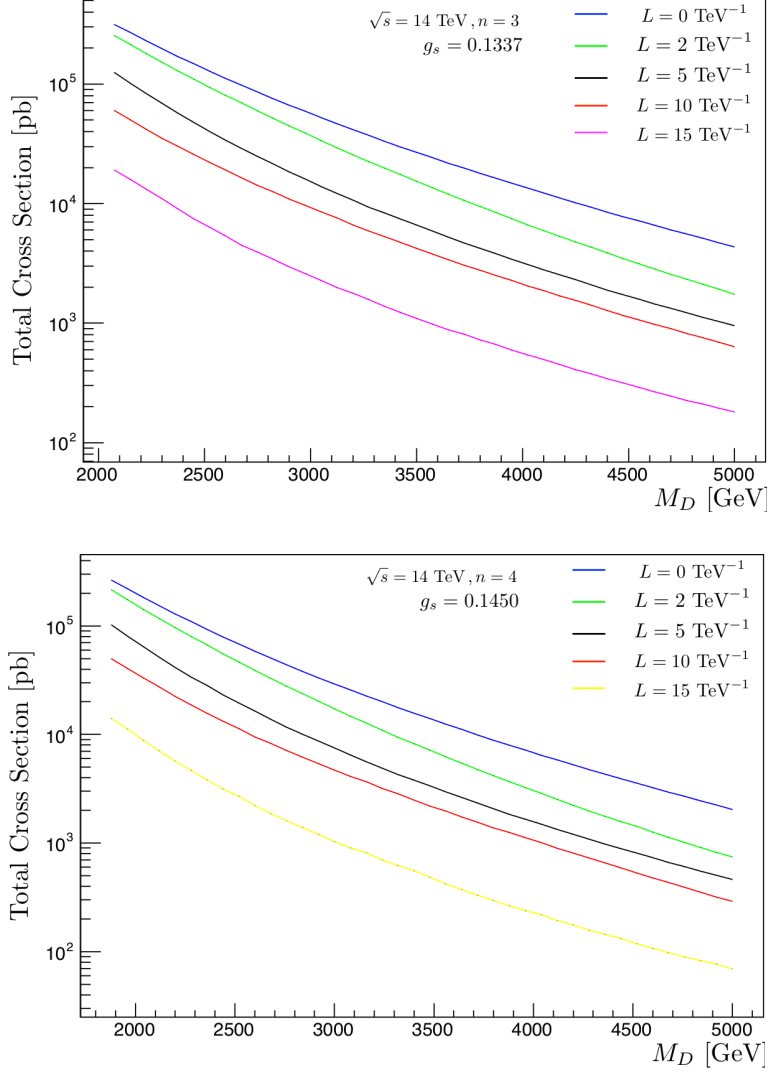


Figure 10. The first plot shows the total cross-section of string ball production for $\sqrt{s} = 14$ TeV, $n = 3$ and $L=0, 2, 5, 10, 15$ TeV^{-1} . The second plot shows the total cross-section of string ball production for $\sqrt{s} = 14$ TeV, $n = 4$ and $L=0, 2, 5, 10, 15$ TeV^{-1} .

for the same value of g_s . The number of extra dimension takes the following values $n = 3, 4, 5, 6$. In the figure 12, we can see that, in the case that the parameter γ changes with the number of dimensions according to the equation (2.6), the cross-section drops while the number of dimensions increases for the same value of the width of the brane.

The figure 13, illustrates the difference of the cross-section of the string ball production between the non-split-fermion and the split-fermion model. We see the drop of the cross-section in the case of the two-dimensional split fermion model by calculating the ratio of the cross-section for $L = 0$ to $L = 10$ and 15 TeV^{-1} . By comparing the graphs in figure 13, we can see how the ratio of the cross-section for string ball production in the non-splitting case to the splitting case depends on the number of extra dimensions. However, the ratio increases at least by a factor of two while the width of the brane increases.

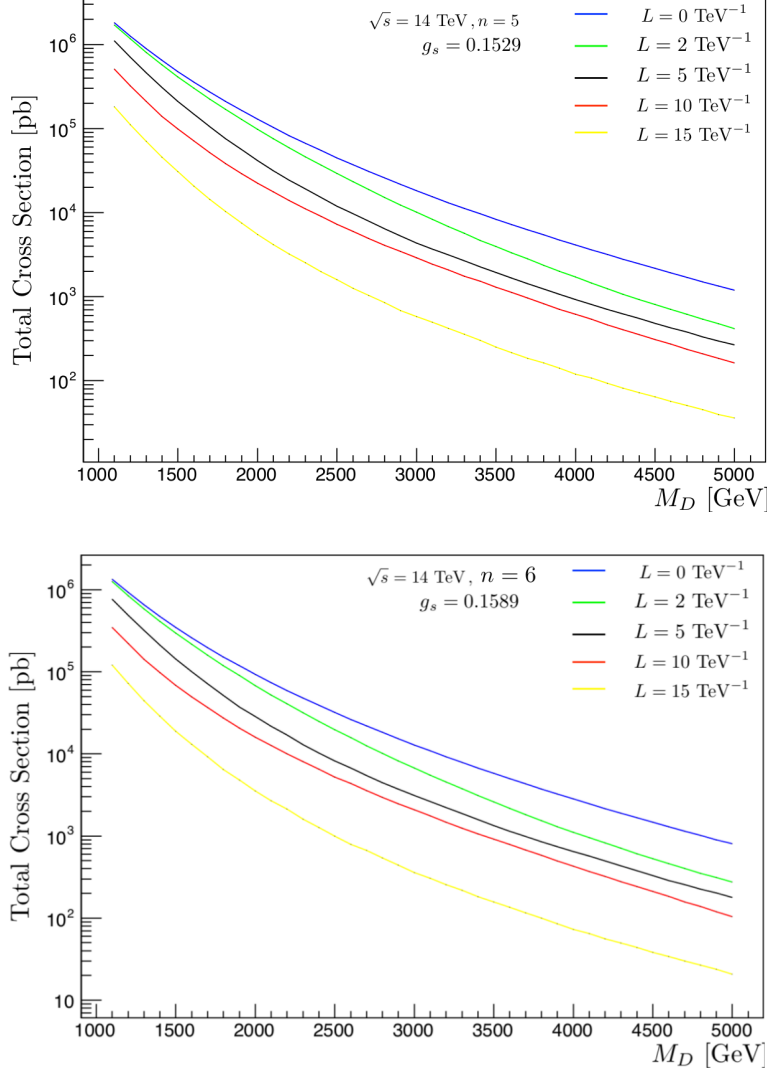


Figure 11. The first plot shows the total cross-section of string ball production for $\sqrt{s} = 14$ TeV, $n = 5$ and $L=0, 2, 5, 10, 15$ TeV^{-1} . The second plot shows the total cross-section of string ball production for $\sqrt{s} = 14$ TeV, $n = 6$ and $L=0, 2, 5, 10, 15$ TeV^{-1} .

In figure 14, we illustrate the dependence of the black hole production cross-section in various number of extra dimensions $n = 5, 6$ and different value of L ($L = 0, 5, 10, 15$ TeV^{-1}).

The figures 15–17, illustrate the threshold for the fundamental Planck scale M_D , where the production cross-section drops below 10^{-1} fb, 1 fb, and 10 fb for different values of L . Such figures are very helpful for comparing the threshold M_D for split-fermion to non-split-fermion models as a function of L . In these figures, the error in the value of M_D is ± 5 GeV. In figures 15 and 16, we consider $n = 5$. In figure 17, we consider $n = 5$ and $n = 6$ and centre-of-mass energy 8 TeV and 14 TeV. From the figure 17, we can see that, while the number of extra dimensions increases, the the fundamental Planck scale M_D where the production cross-section drops below 10^{-1} fb, decreases. We do not have threshold for

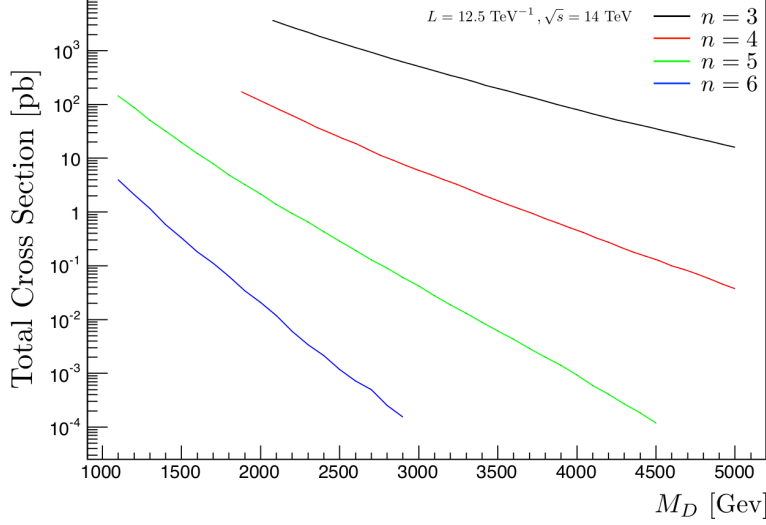


Figure 12. Total cross-section of string ball production for $L=12.5 \text{ TeV}^{-1}$, $\sqrt{s} = 14 \text{ TeV}$, for different number of extra dimensions while parameter γ varies with respect to dimensions. From the top the values of g_s are the following: 0.1836, 0.2636, 0.3355, 0.3986.

the string ball production because it is g_s -dependent therefore model dependent. One can choose a specific g_s and create the threshold for the string ball or to do it for the different values of g_s . Last but not least in figure 18, we consider the cross-section for string ball and black hole production in the case that $M_{\min}^c = M_{\min}^s = 3M_D$. This last figure illustrates that for $M_{\min}^c = 3M_D$ as compared to $M_{\min}^c = 5M_D$ black hole production is larger and string ball production will be slightly smaller.

4 Conclusion

One of the predictions of the TeV-scale gravity models is the possibility of black hole production in proton-proton collisions at the LHC. In order to make serious predictions, one needs to work within the context of realistic phenomenologically valid models. We consider that, a two-dimensional split fermion model is such a model for a TeV-scale quantum gravity. Since, it is the one that produces the correct quark masses and the mixing angles, as well as the required strength of CP violation in quark sector. Because of the correspondence between black holes and string balls, black hole production is dual to the production of a highly-excited long string state. In this paper, we presented cross-sections for the black hole and string ball production for a TeV-scale gravity model with split fermions in two dimensions. We compared the cross-section for black hole and string ball production in proton-proton collisions in the non-split-fermion model to a two-dimensional split-fermion model. We conclude with the following comments:

1. The cross-section of the string ball production is higher than the black hole especially for g_s less than 0.25.

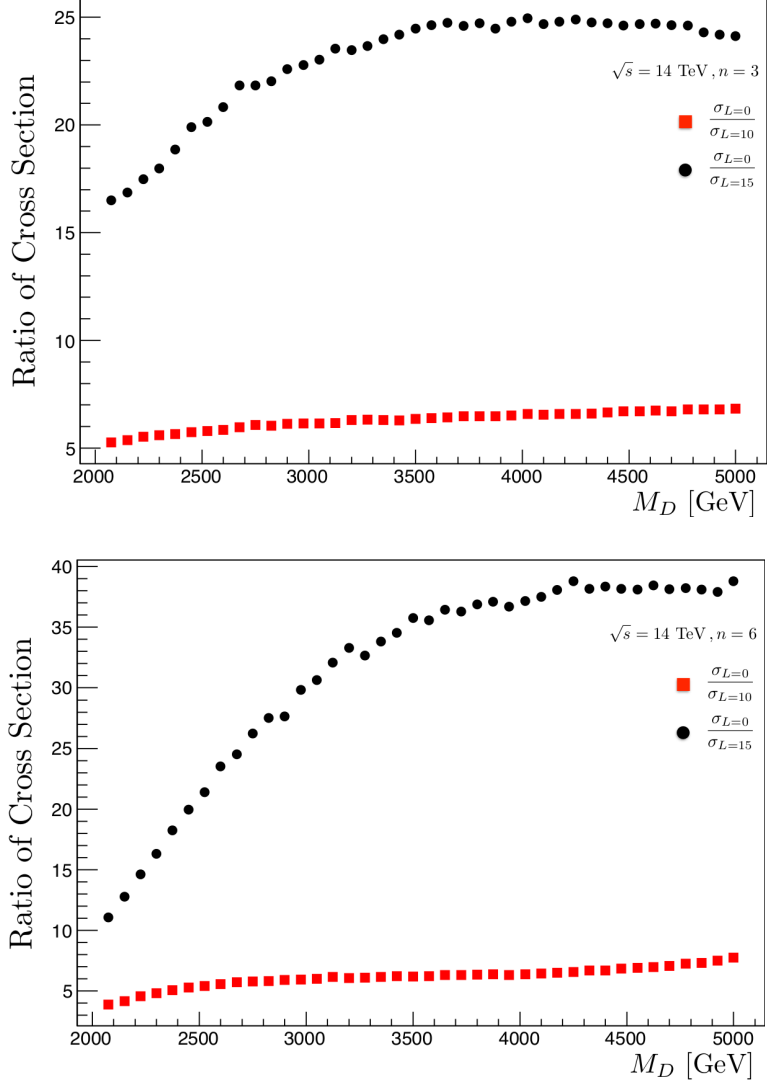


Figure 13. Ratio of string ball production for non split case to the string ball production for two-dimensional split fermion model. The first plot shows the ratio for $n = 3$ and $g_s = 0.1337$. The second plot shows the ratio for $n = 6$ and $g_s = 0.1589$.

2. The cross-section of the black hole or the string ball production drops while the width of the brane increases. The last feature is obvious in the figure 13, where we see the drop of the cross-section to be by a factor of at least two with the increase of the width of the brane from $L = 10$ to 15 TeV^{-1} .
3. The cross-section for string ball production in two-dimensional split fermion model reduces more in comparison to black holes.
4. Black hole is quite hard to be observed at the LHC. In particular, for $\sqrt{s} = 14 \text{ TeV}$ and in the case that the fundamental Planck scale is greater than the current experimental limits [51], black holes cannot be produced at the LHC. In the figure 14, we illustrate that in order to have cross-section greater than 10^{-3} pb , M_D must

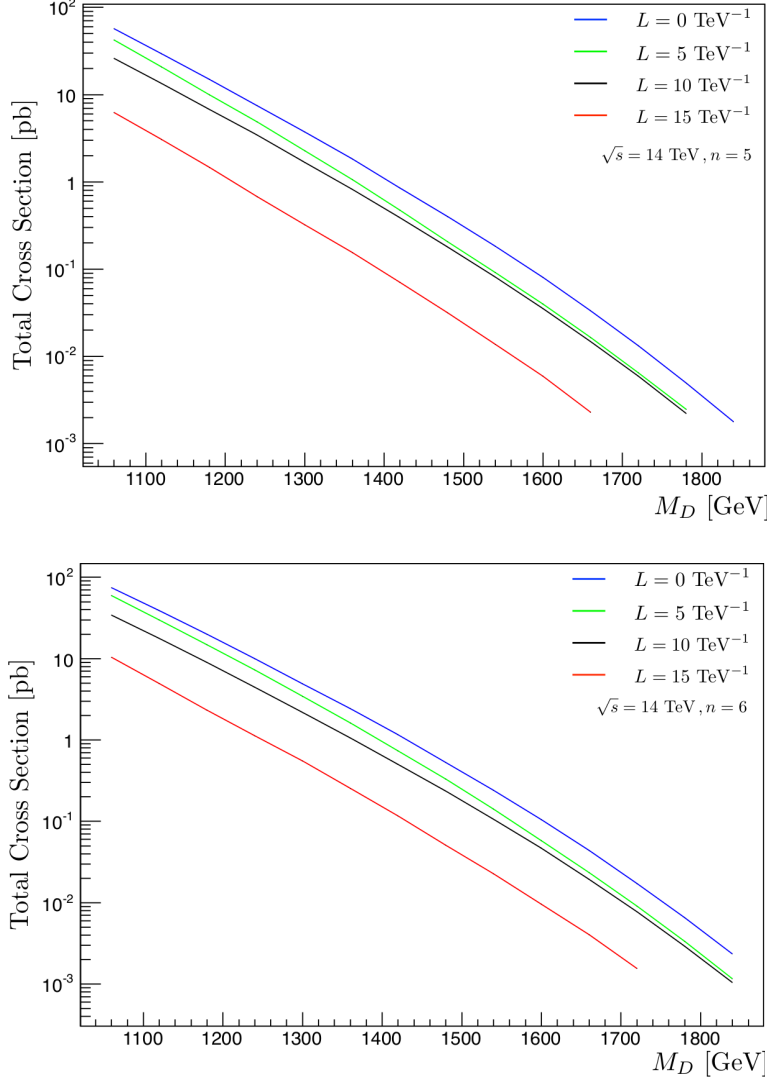


Figure 14. The first plot shows the total cross-section of black hole production for $\sqrt{s} = 14$ TeV, $n = 5$ and $L=0, 5, 10, 15$ TeV^{-1} . The second plot shows the total cross-section of black hole production for $\sqrt{s} = 14$ TeV, $n = 6$ and $L=0, 5, 10, 15$ TeV^{-1} .

be less than or near 1.8 TeV. In the case of centre-of-mass energy 8 TeV, in order to have cross-section greater than 10^{-4} pb, M_D must be less than or near 1.3 TeV as it is illustrated in figure 8. Note that, the actual value of M_D where the cross-section drops below any value depends on the width of the brane. Such that the thicker the brane, the smaller the value of M_D where the cross-section drops below any given value.

5. Cross-section for string ball depends significantly on string coupling constant, making it very model dependent. We suggest that using the current data of the LHC at 8 TeV perhaps, one can already rule out some range of the parameter space. According to ATLAS and CMS collaborations results [39, 44], no string balls or black holes have

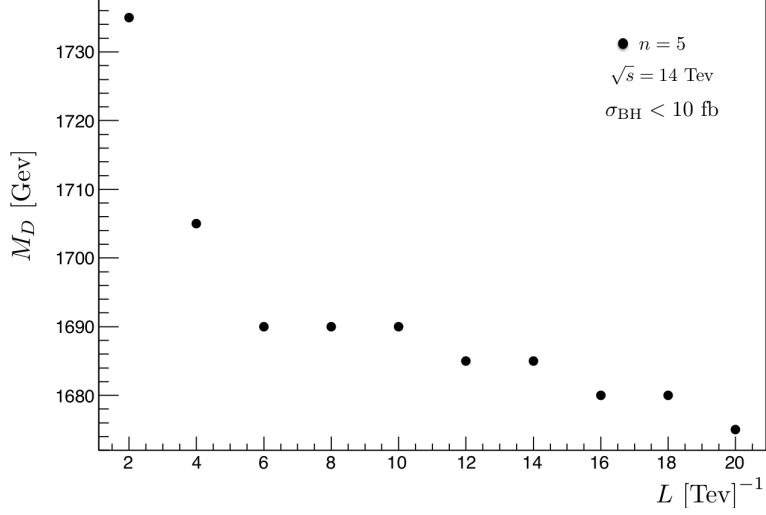


Figure 15. Threshold for black hole production for $n = 5$ and $\sqrt{s} = 14$ TeV. In this plot the limit for the cross-section is 10 fb.

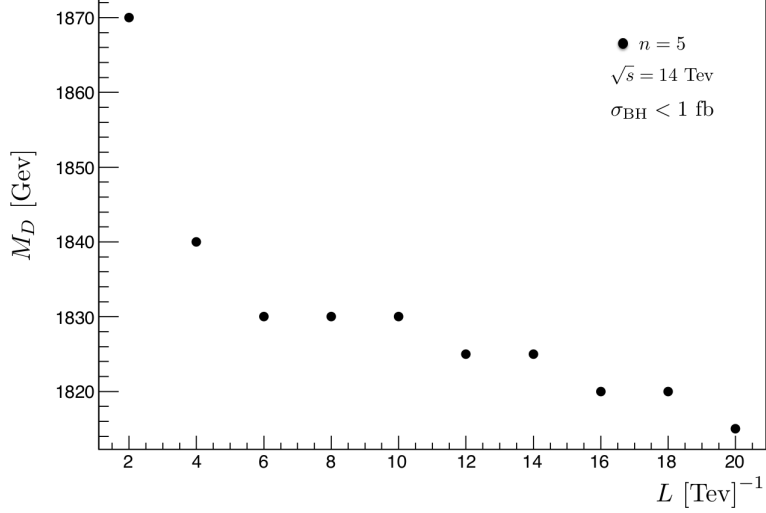


Figure 16. Threshold for black hole production for $n = 5$ and $\sqrt{s} = 14$ TeV. In this plot the limit for the cross-section is 1 fb.

been observed which lead us to conclude, if we still want to believe in string ball model, then, the value of the string coupling constant in six dimensions is close to or larger than $g_s = 0.3986$ which we take into account for one of the plots in figures 4–6. Even then, the value of cross-section for string ball production is high, unless one considers a proper range of M_D , or a very thick brane.

- Given the lack of signature of black holes or string balls for the centre-of-mass energy $\sqrt{s} = 8$ TeV at the LHC, limits on the value of the fundamental Planck scale can be imposed. These limits depend on the width of split fermion dimension and the value of the string coupling constant. In particular, comparing the black line in figure 6 and

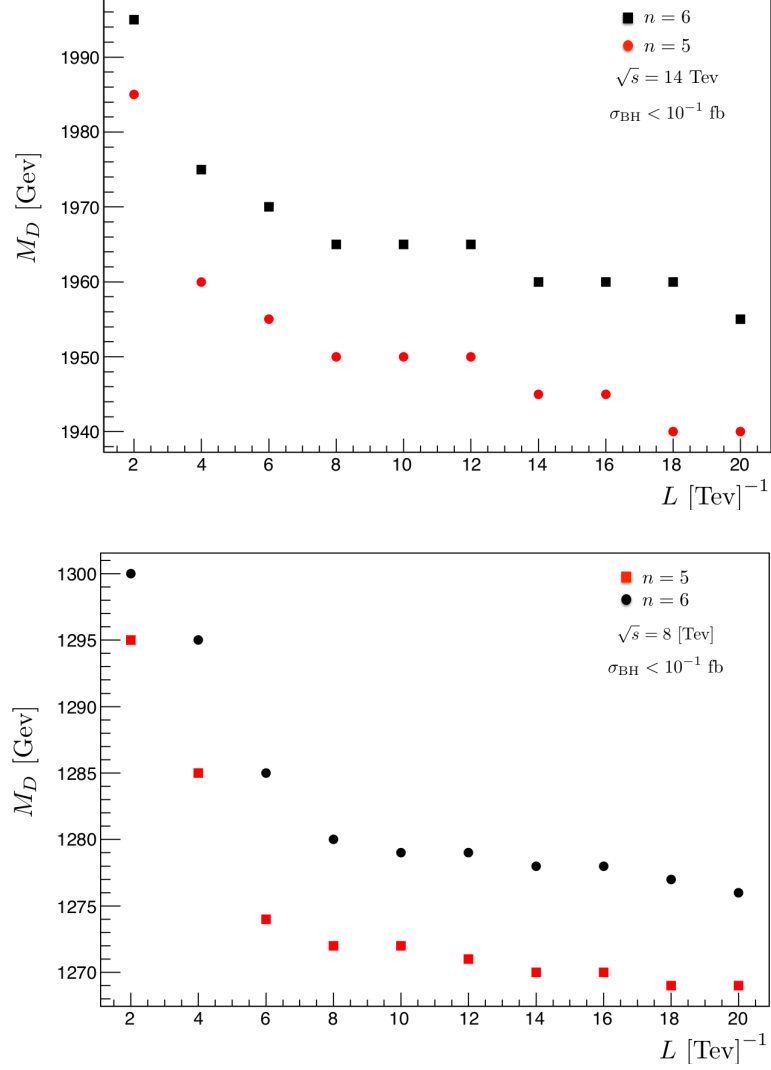


Figure 17. The first plot shows the threshold for black hole production for $\sqrt{s} = 14$ TeV. In this plot the limit for the cross-section is 10^{-1} fb. The second plot shows the threshold for black hole production for $\sqrt{s} = 8$ TeV. In this plot the limit for the cross-section is 10^{-1} fb.

the green line in 4, we see that, for the case $L = 0$ TeV $^{-1}$ in order the cross section to drop below 0.1 fb the value of the fundamental Planck scale of our world should be greater than 2.2 TeV while, for the case $L = 15$ TeV $^{-1}$, $M_D > 1.9$ TeV.

7. As we can see from figure 7, if one wishes to have cross-section for production of string balls less or close to 1 fb even for $M_D = 1$ TeV, one has to consider a two-dimensional split fermion model with extremely thick brane. In such a model, one can explain the lack of signature of string balls at the LHC.
8. From figures 4–6, we see that, in six extra dimensions, if $M_D \geq 2.51$ TeV, in the case that, g_s is given by equation (2.7), (or when parameter γ is given by equation (2.6)), then, string balls cannot be observed at the LHC for $\sqrt{s} = 8$ TeV. This is also valid

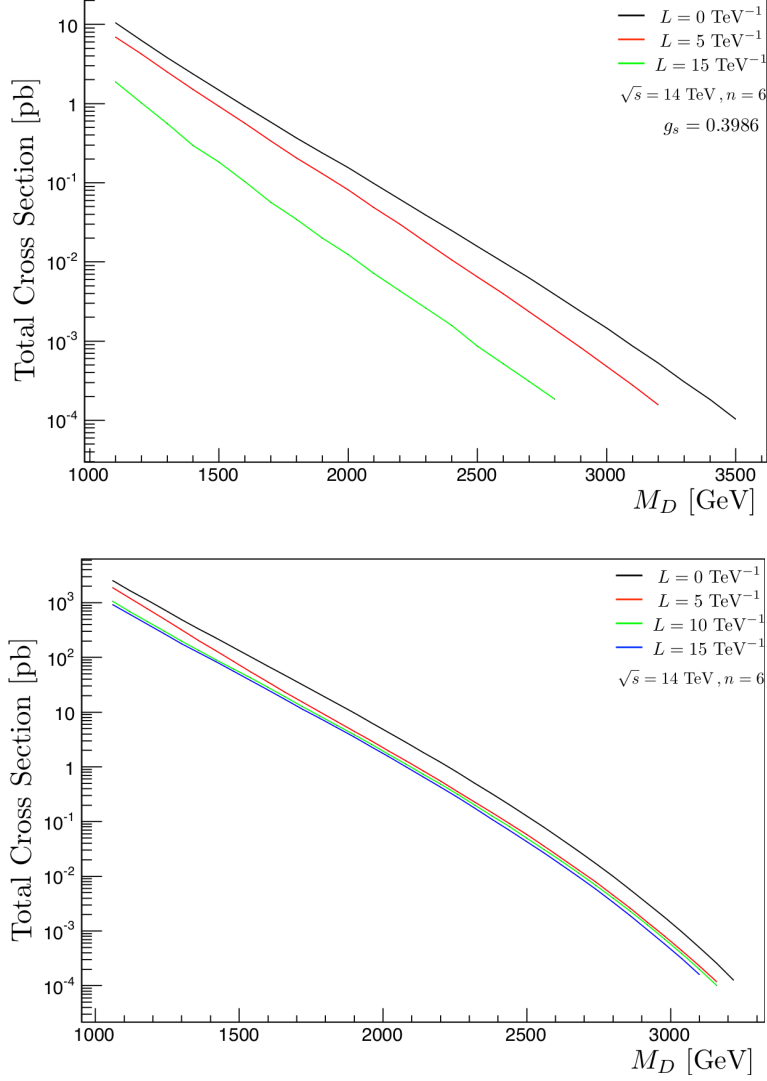


Figure 18. The first plot shows the total cross-section of string ball production for $\sqrt{s} = 14 \text{ TeV}$, $n = 6$ and $L=0, 5, 15 \text{ TeV}^{-1}$. The second plot shows the total cross-section of black hole production for $\sqrt{s} = 14 \text{ TeV}$, $n = 6$ and $L=0, 5, 10, 15 \text{ TeV}^{-1}$.

if g_s is near the value coming from equation (2.7).

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A Appendix

In this appendix, we give some of the details about the parameter file. There are three categories of variables in the parameter file.

1. The variables that, we do not take into account because they do not affect the cross-section for the formation of the black hole but, the evaporation part.
2. The variables that, we take into account but, they are fixed for all of our figures.
 - Incoming particles: For this parameter we set the value to be always 1 since we take into account proton-proton collisions.
 - Definition of M_{pl} : Also, here the value is always 1 because we use the PDG definition of the Planck mass [54].
 - Choose a case: Here we choose the case of tensionless non-rotating black hole. Therefore, the value we consider is 1 as well.
 - Number of splitting dimensions: The model we consider here is a two-dimensional split fermion model. Thus, the value of this parameter should be equal to 2.
 - Tension: As we have mentioned we take into account tensionless non-rotating case. Therefore, the value of this parameter is 1.0.
 - Choose a pdf file: We consider the CTEQ parton distribution functions so, the value should be from 200 to 240. We chose this value to be 200.
 - Other definition of cross-section: We do not want to have any other definition of the cross-section beside the default one. We set the value of this parameter equal to 0.
 - Calculate the cross-section according to: We want calculation of the cross-section according to the radius of initial black hole so, we choose this value to be 0 as well. For this case, the cross-section is calculated in the same way as in [53].
 - Mass, momentum, angular momentum loss factor: We consider only 10% loss of the mass, momentum, and angular momentum. So, the values for these three different parameters are 0.1.
3. The variables that, we take into account but, they change for every different graphs or for every different run of BlackMax code.
 - Number of extra dimensions.
 - Maximum mass: In the black hole case we have this upper limit equal to the centre-of-mass energy. In the string ball case we set this limit equal to $5M_D$ unless $5M_D > \sqrt{s}$ where the maximum mass will be the energy of centre-of-mass. Note that, $5M_D = M_s/g_s^2$. If one wants to investigate the cross-section of black hole and string ball production together then, this limit must be set equal to the centre-of-mass energy (\sqrt{s}). We do not consider this case in this paper.

- Minimum mass: In the black hole case this limit is equal to $5M_D$. In the string ball case we consider the minimum mass to be $3M_s$. If one wants to investigate the cross-section of black hole and string ball production together then, this limit must be set equal to $3M_s$.
- centre-of-mass energy of incoming particle.
- Include string ball.
- M_{pl} : This parameter must be entered in units of GeV.
- String scale (M_s).
- String coupling (g_s).
- Split fermion width and location: The split-fermion width w is defined in accordance to the Gaussian wave function of the form

$$\exp\left(-\frac{2x^2}{w^2}\right). \quad (\text{A.1})$$

Thus, if one uses the form $\exp(-x^2\mu^2)$ for the Gaussian profile in accordance to Eq. (2.1) then, the split-fermion width in BlackMax is $w = \sqrt{2}/\mu$, which must be entered in unit of $1/M_D$,

$$w = \frac{\sqrt{2}L}{c}. \quad (\text{A.2})$$

The location of the quarks is given in the table 1 in units of the μ^{-1} , but we need to enter them in units of $L/30$ in the BlackMax code. If we take into account that,

$$\mu^{-1} = \frac{L}{c}, \quad (\text{A.3})$$

and consider $c = 30$ we end up to enter the location of the particles as they are in the table 1. In the case that, $c \neq 30$ one takes a dimensionless number from table 1 and multiplies it by $30/c$ in order to enter the correct locations of quarks into the parameter file.

- Extra dimension size: A very tricky part of the parameter file is the value of the “Extra dimension size”. We should stress here that it is different from the “size of brane” parameter. Extra dimension size is a parameter that concerns someone who works on the no splitting case. For example, if the number of the splitting dimensions is 2 and total number of extra dimensions is 4. Then, the first two space dimensions use the width of the split brane. The other two directions use this parameter as its brane size. If there is no splitting brane, then this parameter is the only functioning parameter. We keep the value of this parameter fixed and equal to 1 in unit of $1/M_D$. The parameter L must be entered in the line corresponding to the extra-dimension size in units of $1/M_D$. In our case, we first choose M_D and L . Then if, for example, $M_D = a$ GeV, and $L^{-1} = b$ TeV, one has to enter in the parameter file

$$L = \frac{a}{1000b} \frac{1}{M_D}. \quad (\text{A.4})$$

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